

Relational Relativity

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Abstract

According to a simple model of inertia a Machianized theory of special and general relativity named as relational relativity is presented.

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I. Introduction

The famous issues of Newtonian absolute space and time were followed by many constructive critiques of relationalists. The most efficient works of this kind were due to the Ernst Mach, the contemporary physicist and philosopher[1]. Various aspects of Mach's ideas concerning the motion, from Newton's bucket to quantum gravity, has been collected in the proceeding of the conference held at Tübingen (July 1993) for this purpose[2].

In his critique of Newtonian mechanics(NM), Mach arrived at the following two conclusions:

- i) - Only the relative motion of a body with respect to other bodies is observable, not motion with regard to absolute space.
- ii) - The inertial motion of a body is influenced by all the means in the Universe.

To appreciate fully these two physically pleasant ideas we have applied them in a proposed classical model of inertia[3]. In this model we consider the inertia as a real two body interaction which is proportional to the relative acceleration and inertial charges of two bodies

$$\vec{F}_{inertia} = \mu.c_1.c_2(\vec{a}_1 - \vec{a}_2) \quad (1)$$

where μ is a coupling constant , c_1 and c_2 represent the inertial charges of particles 1 and 2 respectively and $(\vec{a}_1 - \vec{a}_2)$ is their relative acceleration with respect to each other. Then in a system consisting of N particles the total force imposed on the particle labeled i is :

$$\vec{F}_i = \mu.c_i \sum_{j=1}^N c_j(\vec{a}_i - \vec{a}_j) \quad (2)$$

where the index i refers to the particle i and the summation is done over all particles. By definition in the real world the inertial charge and the Newtonian inertial mass of a particle are related as follows:

$$m_i = \mu.c_i \sum_{j=1}^{all} c_j. \quad (3)$$

Summation is taken over all particles in the Universe. This means that the inertial mass of a particle (say labeled j) is determined not only by its own feature (c_j) but is also a global effect of all particles in the world($\sum_{j=1}^{all} c_j$) . This may be considered as a simple formulation of Mach's idea about inertia. Since local inhomogenities have no observed effects on the inertial mass then it is accepted that the inertial mass is determined by the global structure of the Universe and this is exactly expressed by the relation(3). If we rewrite the equation(2) in terms of the inertial masses then a modified form of the Newton's second law is obtained, i.e.,

$$\vec{F}_i = m_i \left(\vec{a}_i - \frac{\sum_{j=1}^{all} m_j \vec{a}_j}{\sum_{j=1}^{all} m_j} \right) \quad (4)$$

As it is evident these equations are invariant under a more general coordinate transformations S' than Galili. These transformations may be called generalized Galilian transformations with the form:

$$\begin{cases} t' = t \\ \vec{a}' = \vec{a} - \vec{b} \\ \vec{u}' = \vec{u} - \vec{b}t - \vec{v} \\ \vec{x}' = \vec{x} - \frac{1}{2}\vec{b}t^2 - t\vec{v} + \vec{x}_0 \end{cases} \quad (5)$$

where \vec{b} , \vec{v} and \vec{x}_0 are constant acceleration, velocity and position of S' with respect to S at $t = 0$ respectively.

Eq.(4) in turn leads to some full Machian results. The one which is of interest here is that the so-called absolute space is just the frame attached to the center of mass of the universe in which the Newtonian second law, $\vec{F}_i = m_i \vec{a}_i$ is recovered. The main feature of this model from a Machian point of view is its relational nature, so that the presence of each particle in the Universe and its location relative to the others determine the inertial reference frames. It is seen that Eqs. (2) and (4) also satisfy Newton's third law automatically. For a two particle system we have $\vec{F}_1 = -\vec{F}_2$ and for a system with N particles they make $\sum_{i=1}^N \vec{F}_i = 0$.

We may also extend this model to gravity. Equivalence principle here means that the source of inertia and gravitation is the same. Let us define the gravitational force between two particles of inertial charges c_1 and c_2 as:

$$|\vec{F}_G| = \frac{\mu^2 \cdot c_1 \cdot c_2}{|\vec{r}_{12}|^2} \quad (6)$$

Then we can express gravitational constant G in terms of inertial charges c_i s;

$$G = \left(\sum_{j=1}^{all} c_j \right)^{-2} \quad (7)$$

or in other form

$$G = \frac{\mu}{\sum_{j=1}^{all} m_j} \quad (8)$$

Eqs. (7) and (8) show that G as a global effect is resulted from all inertial charges and as an indirect result $\sum_{j=1}^{all} c_j$ is finite. According to the Mach's ideas the so-called physical constants (including G) should be determined from global features of the universe. Thus Eqs. (7) and (8) reveal the very feature of a good Machian model.

The Lagrangian function from which Eq.(4) may be extracted is simply obtained by following the canonical procedure of D'Alembert's principle. Starting from Eq.(4) and restricting ourselves to systems for which the virtual work of the forces of constraint vanishes we obtain

$$\sum_i \left[\vec{F}_i - m_i \left(\vec{a}_i - \frac{\sum_{j=1}^{all} m_j \vec{a}_j}{\sum_{j=1}^{all} m_j} \right) \right] \cdot \delta \vec{r}_i = 0, \quad (9)$$

which is the new form of D'Alembert principle. Here $\delta\vec{r}_i$ s are infinitesimal changes of coordinates as the result of virtual displacement of the system. This leads to the result just like the one in ordinary NM except that the kinetic energy T which is equal to $\sum_i \frac{1}{2}m_i v_i^2$ should be replaced by this form:

$$\begin{aligned} T &= \sum_i \frac{1}{2}m_i v_i^2 - \frac{\left[\sum_i m_i v_i\right]^2}{2\sum_i m_i} \\ &= \frac{1}{4} \sum_i \sum_j m_i m_j \frac{(\vec{v}_i - \vec{v}_j)^2}{\sum_k m_k} \end{aligned} \quad (10)$$

Indeed the difference is the second term in the first row and is just the kinetic energy of the center of mass which is canceled out in this model. This is well justified when is applied in cosmology. When we are dealing with the whole Universe motion and kinetic energy of its center of mass have no physical meaning.

The new form of T as a function of the magnitude of relative velocities of particles has a scalar invariant manner. Then as an other advantage in this model the Lagrangian (and Hamitonian) of a system are scalar invariants from point of view of a nonrotating observer.

$$L = \frac{1}{4} \sum_i \sum_j m_i m_j \frac{(\vec{v}_i - \vec{v}_j)^2}{\sum_k m_k} - V(r_{ij}) \quad (11)$$

It is noticeable that in a different way to obtain a relational NM Eq.(11) has been proposed by Lynden-Bell[4,5].

We may summarize the Machian features of this model as follows:

1. The relational nature of this model is so that by considering relational distances there is no need to assume absolute space or inertial frame. Indeed the so-called inertial frame is the frame attached to the center of mass of the Universe. Then existance of each particle and its location with respect to others determine the inertial frames.
2. Inertial mass of each particle depends on its own inertial charge and the sum of inertial charges of all particles in the world. Then it is not a natural constant, and may change whenever the total inertial charge of the world undergoes any change(e.g. in pair production era).

3. Gravitational constant G is related to the sum of all inertial charges existing in the Universe and as a global effect individual particles share in its construction. Just like inertial mass, this may be changed whenever the total inertial charge of the world faces with changes.
4. The concept of energy in this model is independent of measuring reference frame and is an invariant scalar quantity.
5. For an empty universe predicts no structure.

Collection of these features in the above model provides us a suitable guide to continue and achieve a modified theory of relativity, i.e. a theory of relativity without any non-Machian shortcoming, what we may call as relational relativity(RR). As a first step toward RR it is convenient to begin with special relativity (SR).

II. Relational Special Relativity

At the beginning it should be noticed that according to the results (7) and (8) it is possible to assume a world without inertia via vanishing the coupling constant μ , but the assumption of a world without gravitation is physically impossible. Then the subject of special relativity because of its ignorance of gravitation is under question and cannot be considered as a global theory from a Machian stand point. In spite of this we try to present a relational special theory of relativity.

Although Michelson-Morley experiment rejects the concept of ether but SR still is based on the same assumption of the existence of absolute space and preference of inertial frames as NM. In a relational approach we may remove the need for absolute space in SR. To do this task some preliminary remarks should be mentioned. In NM the Lagrangian of a free particle is just the kinetic energy then its action is

$$S = \int dt \left(\frac{1}{2} m \dot{x}^2 \right). \quad (12)$$

where \dot{x} is the velocity of the particle with mass m . In SR this is changed to the following form

$$S = -m \int dt (1 - \dot{x}^2)^{\frac{1}{2}} = -m \int ds \quad (13)$$

so that in low velocity limit ($\dot{x} \ll 1$) the equation of motion returns to the Newtonian form. Other form of this relation in terms of space-time metric is

$$S = -m \int dt \left(g_{\mu\nu} \frac{dx^\mu}{dt} \frac{dx^\nu}{dt} \right)^{\frac{1}{2}}. \quad (14)$$

That is the Lagrangian is as follows

$$L = -m(g_{\mu\nu}\dot{x}^\mu\dot{x}^\nu)^{\frac{1}{2}} \quad (15)$$

where $g_{\mu\nu} = \eta_{\mu\nu}$ i.e. just the Minkowski metric.

According to the definition of canonical momentum we have

$$p_\alpha = \frac{\partial L}{\partial \dot{x}^\alpha} = -\frac{m\eta_{\alpha\mu}\dot{x}^\mu}{(\eta_{\mu\nu}\dot{x}^\mu\dot{x}^\nu)^{\frac{1}{2}}} = -m\eta_{\alpha\mu}u^\mu \quad (16)$$

where by definition $\frac{dx^\mu}{ds} = u^\mu$.

Then the equation of motion has the form

$$m\dot{u}_\alpha = 0. \quad (17)$$

Extension of the above problem to a system of N particles with masses m_a , $a = 1, 2, \dots, N$ is made by defining the action as

$$S = -\sum_{a=1}^N m_a \int (\eta_{\mu\nu} \frac{dx_a^\mu}{dp} \frac{dx_a^\nu}{dp})^{\frac{1}{2}} dp \quad (18)$$

where p is an affine parameter and the Lagrangian is

$$L = -\sum_{a=1}^N m_a (\eta_{\mu\nu} \frac{dx_a^\mu}{dp} \frac{dx_a^\nu}{dp})^{\frac{1}{2}}. \quad (19)$$

With what has been mentioned we may add two other primary remarks about geometrical and physical points. With physical point we mean a point mass but a geometrical point need not contain any matter. We should insist in this fact that a distance measurement is only made between two physical points. So in presenting the line element definition instead of measuring the distance of physical points with respect to an arbitrary origin we should define it in terms of the distance between physical points (or physically significant points e.g. center of mass of a system). Certainly this definition has higher Machian(Relational) validity.

Now from this point of view let us define the line element ds_a^2 for a noninteracting N particle system as

$$ds_a^2 = \eta_{\mu\nu} \left(dx_a^\mu - \frac{\sum_b m_b dx_b^\mu}{\sum_b m_b} \right) \left(dx_a^\nu - \frac{\sum_b m_b dx_b^\nu}{\sum_b m_b} \right) \quad (20)$$

where index (a) refers to the particle labeled (a) .

Then the related action and Lagrangian are as follows

$$S = - \sum_a m_a \int [\eta_{\mu\nu} (\frac{dx_a^\mu}{dp} - \frac{\sum_b m_b \frac{dx_b^\mu}{dp}}{\sum_b m_b}) (\frac{dx_a^\nu}{dp} - \frac{\sum_b m_b \frac{dx_b^\nu}{dp}}{\sum_b m_b})]^\frac{1}{2} dt \quad (21)$$

$$L = - \sum_a m_a \left[\eta_{\mu\nu} \left(\frac{dx_a^\mu}{dp} - \frac{dx_{cm}^\mu}{dp} \right) \left(\frac{dx_a^\nu}{dp} - \frac{dx_{cm}^\nu}{dp} \right) \right]^\frac{1}{2}. \quad (22)$$

The canonical momentum of the k th particle is

$$\begin{aligned} (p_k)_\alpha &= \frac{\partial L}{\partial \frac{dx_k^\alpha}{dp}} = -\eta_{\alpha\nu} m_k \frac{(\frac{dx_k^\nu}{dp} - \frac{dx_{cm}^\nu}{dp})}{\frac{ds_k}{dp}} \\ &= -\eta_{\alpha\nu} m_k (u_k^\nu - u_{cm}^\nu) \\ &= -m_k ((u_k)_\alpha - (u_{cm})_\alpha). \end{aligned} \quad (23)$$

Since $\frac{\partial L}{\partial x_k^\alpha} = 0$ and $\frac{d}{dp}(p_k)_\alpha = -m_k \eta_{\alpha\nu} (\frac{du_k^\nu}{dp} - \frac{du_{cm}^\nu}{dp})$, then the equation of motion of the k th particle is

$$\frac{d\vec{u}_k}{dp} - \frac{d\vec{u}_{cm}}{dp} = 0 \quad (24)$$

which is just the same as the modified form (4) in the Newtonian limit.

The Lagrangian (22) is written without any coordination with respect to a priori fixed virtual absolute space and these are particles by their own relative locations that determine it. This is free from that non-Machian aspects suffering the standard SR. So we may call the relativistic theory based on this Lagrangian as relational special relativity.

III. Relational General Relativity

It seems the same approach may be followed to obtain the relational GR. But this is not so straight forward. Because to extrapolate this result to GR, i.e. to change the Minkowskian flat spacetime $(\eta_{\mu\nu})$ into the Riemannian curved spacetime $(g_{\mu\nu})$, care should be taken of dealing with vector quantities. Summation of the vectors in this case needs parallel transportation of them which in turn requires to define the path of transportation for each of them. Then to achieve a relational theory of GR it requires to choose another strategy with some different approach as follows.

Initially we remark the center of mass(CM) concept in NM. With the help of this concept in the Euclidian space NM of a single particle can be extrapolated and be

applied to a system with N particles. The classical meaning of CM losses its uniqueness when enters in the realm of relativity so that different observers find different points as CM of a given system. The important point worthy to notice about CM is its dual character from a Machian point of view so that despite of its great value as a technical tool to present the relational motion on the other hand as a point in which total mass of the system is located and its motion is to be considered is quite invalid and anti-Machian concept. For a single point has no motion and no inertia.

Turning back to the NM we may define the center of inertial charge (CI). By definition:

$$\begin{aligned} X_{CI}^\mu &= \frac{\sum_i \sum_j c_i c_j (x_i^\mu + x_j^\mu)}{2(\sum_j c_j)^2} \\ &= \frac{\sum_i m_i x_i^\mu}{\sum_i m_i} = X_{CM}^\mu \end{aligned} \quad (25)$$

where X_{CM}^μ and X_{CI}^μ are coordinates of CM and CI respectively. As it is evident the concept of CI has also a mutually relational content between particles.

Now it is easy to show that the result (4) may be obtained with the help of Lagrangian formalism in NM and imposing the following condition on CI;

$$\delta X_{CI}^\mu \equiv 0 \quad (26)$$

Because

$$\delta X_{CI}^\mu = \sum_i m_i \delta x_i^\mu = 0, \quad (27)$$

and imposing this by using the method of undetermined Lagrangian multipliers in variations of the action of a system with N noninteracting particles, yields:

$$\delta I = \sum_n \int dt [m_n \ddot{x}_n^\mu + f m_n] \delta x_n^\mu \equiv 0 \quad (28)$$

where the coefficient f is determined as follows:

$$f = - \frac{\sum_n m_n \ddot{x}_n^\mu}{\sum_n m_n} \quad (29)$$

Thus the equation of motion (4) is obtained. Also with consideration of the condition (27) in variation of the action (18) in special relativity the result (22) is derived.

Then to remove the Machian objection to the concept of CM the following condition as a Machian condition may be imposed to the variations of the dynamical variables x_n^μ of the system. Let us first define X^μ as

$$X^\mu \equiv \sum_n m_n x_n^\mu \quad (30)$$

Of course X^μ is not a vector quantity and depend to the chosen reference frame. Then we denote its variations with δX^μ :

$$\delta X^\mu \equiv \sum_n m_n \delta x_n^\mu \quad (31)$$

Here δX^μ is not vector while δx_n^μ s are vectors. Similarly δX_μ is defined as follows:

$$\delta X_\mu \equiv \sum_n m_n g_{\mu\lambda}(x_n) \delta x_n^\lambda \quad (32)$$

Now as a Machian principle we postulate that allways δX_μ vanishes (lower index is chosen only for convenience). This means that variations of dynamical variables x_n^μ are under the following condition:

$$\sum_n m_n g_{\mu\lambda}(x_n) \delta x_n^\lambda = 0 \quad (33)$$

Despite of this fact that (33) is not a covariant condition we can make the best use of it to find at least a clue for the geodesic equations in GR.

Matter action for a system consisting of n particles with masses m_n is given by the following form in GR;

$$I = \sum_n m_n \int dp \left(g_{\mu\nu}(x_n(p)) \frac{dx_n^\mu(p)}{dp} \frac{dx_n^\nu(p)}{dp} \right)^{\frac{1}{2}} \quad (34)$$

where p is some quantity that simultaneously parametrizes all the space-time trajectories of the various particles.

Variation of the action (34) due to an infinitesimal variation in the dynamical variables $x^\mu \rightarrow x^\mu(p) + \delta x^\mu(p)$ is given by:

$$\begin{aligned} \delta I = \frac{1}{2} \sum_n m_n \int dp & \left[g_{\mu\nu}(x_n(p)) \frac{dx_n^\mu(p)}{dp} \frac{dx_n^\nu(p)}{dp} \right]^{-\frac{1}{2}} \\ & \times \left\{ 2g_{\mu\nu}(x_n(p)) \frac{dx_n^\mu(p)}{dp} \frac{d\delta x_n^\nu(p)}{dp} \right. \\ & \left. + \left(\frac{\partial g_{\mu\nu}(x)}{\partial x^\lambda} \right)_{x=x_n(p)} \frac{dx_n^\mu(p)}{dp} \frac{dx_n^\nu(p)}{dp} \delta x_n^\lambda(p) \right\} \end{aligned} \quad (35)$$

It is convenient to change variables of integration (35) from p to the τ_n (the proper time of the particle n) defined by:

$$d\tau_n \equiv (g_{\mu\nu} dx_n^\mu dx_n^\nu)^{\frac{1}{2}} \quad (36)$$

So the integral in (35) may be written in a simpler form:

$$\delta I = \frac{1}{2} \sum_n m_n \int d\tau_n \left\{ 2g_{\mu\lambda}(x_n) \frac{dx_n^\mu}{d\tau_n} \frac{d\delta x_n^\lambda}{d\tau_n} + \frac{\partial g_{\mu\nu}(x_n)}{\partial x_n^\lambda} \frac{dx_n^\mu}{d\tau_n} \frac{dx_n^\nu}{d\tau_n} \delta x_n^\lambda \right\} \quad (37)$$

Finally integration by parts of the first term in (37) with the condition that $\delta x^\mu(\tau_n)$ vanishes on the boundaries of integration yields that :

$$\delta I = \sum_n \int d\tau_n g_{\mu\lambda}(x_n) \left\{ m_n \left(\frac{d^2 x_n^\mu}{d\tau_n^2} + \Gamma_{\rho\sigma}^\mu \frac{dx_n^\rho}{d\tau_n} \frac{dx_n^\sigma}{d\tau_n} \right) \right\} \delta x_n^\lambda \quad (38)$$

where $\Gamma_{\rho\sigma}^\mu$ are the second type Christoffel symbols. Then according to the principle of stationary action, δI vanishes for general variations in the dynamical variables δx_n^λ if and only if the dynamical variables obey the geodesic equations:

$$\frac{d^2 x_n^\mu}{d\tau_n^2} + \Gamma_{\rho\sigma}^\mu \frac{dx_n^\rho}{d\tau_n} \frac{dx_n^\sigma}{d\tau_n} = 0 \quad (39)$$

Now we repeat the above standard process with consideration of the Machian condition (33) to achieve the equations of motion. To impose the mentioned condition with the method of undetermined Lagrangian multipliers it is enough only to add the following term to the variations of the action (34).

$$\int dp f^\mu \sum_n m_n g_{\mu\lambda}(x_n) \delta x_n^\lambda \quad (40)$$

where f^μ s are undetermined coefficients and just as in (34) parameter p is an arbitrary quantity which simultaneously parametrizes the space-time trajectories of different particles. Then we have:

$$\delta I = \sum_n \int dp \left\{ m_n g_{\mu\lambda}(x_n) \left[\frac{\partial p}{\partial \tau_n} \left(\frac{d^2 x_n^\mu}{dp^2} + \Gamma_{\rho\sigma}^\mu \frac{dx_n^\rho}{dp} \frac{dx_n^\sigma}{dp} \right) + f^\mu \right] \right\} \delta x_n^\lambda = 0 \quad (41)$$

With f^μ s determined as:

$$f^\mu = - \frac{\sum_n m_n \frac{\partial p}{\partial \tau_n} \left(\frac{d^2 x_n^\mu}{dp^2} + \Gamma_{\rho\sigma}^\mu \frac{dx_n^\rho}{dp} \frac{dx_n^\sigma}{dp} \right)}{\sum_n m_n} \quad (42)$$

Because of the mean operation over all particles f^μ is a global quantity.

Therefore by inserting the value of f^μ the Machianized form or the relational form of the geodesic equations of motion are derived as follows:

$$\frac{d^2 x_n^\mu}{dp^2} - \frac{\sum_j m_j \frac{\partial \tau_n}{\partial \tau_j} \frac{d^2 x_j^\mu}{dp^2}}{\sum_j m_j} + \Gamma_{\rho\sigma}^\mu \frac{dx_n^\rho}{dp} \frac{dx_n^\sigma}{dp} - \frac{\sum_j m_j \frac{\partial \tau_n}{\partial \tau_j} \Gamma_{\rho\sigma}^\mu \frac{dx_j^\rho}{dp} \frac{dx_j^\sigma}{dp}}{\sum_j m_j} = 0 \quad (43)$$

It reveals that in the weak field limit the equations (43) corresponde with the Newtonian one , because the Christoffel symbols vanish and parameters τ_n in this limit are all the same and are equal to t , then (43) transform to the modified Newtonian form (4).

Now according to the relational result (43) we may propose the covariant form of the geodesic equations as follows:

$$\frac{d^2 x_n^\mu}{dp^2} + \Gamma_{\rho\sigma}^\mu \frac{dx_n^\rho}{dp} \frac{dx_n^\sigma}{dp} - \frac{\sum_j m_j \frac{\partial \tau_n}{\partial \tau_j} U_{x_j}^{x_n} \left(\frac{d^2 x_j^\mu}{dp^2} + \Gamma_{\alpha\beta}^\mu \frac{dx_j^\alpha}{dp} \frac{dx_j^\beta}{dp} \right)}{\sum_j m_j} = 0 \quad (44)$$

where $U_{x_j}^{x_n}$ is the parallel transportation operator from the location of the jth particle to the location of the nth one.

IV. Remarks

We are now staying at a stand point that may return to the famous question that “whether the formalism of general relativity and the Einstein equations are perfectly Machian?” and have a strictly positive answer to it. Because to check the Machian(or anti-Machian) aspects of GR;

1. By now in front of the basic question that why the Einstein field equations have nontrivial solution flat space $R_{\mu\nu} = 0$ for empty universe we had to resort to the boudary conditional reasons. Hereafter, with what we have find about inertia it is seen that the Einstein field equations $\frac{c^4}{8\pi G} R_{\mu\nu} = (T_{\mu\nu} - \frac{1}{2} g_{\mu\nu} T)$ predict $0 = 0$ (instead of $R_{\mu\nu} = 0$) for empty universe. For assuming vacuum T , $T_{\mu\nu} = 0$ makes the RHS of the field equations to be equal zero and on the other side the coupling constant appears on the LHS as G^{-1} , which in turn according to the relations (7) and (8) depends on the existence of all particles in the universe, $G \propto \frac{1}{\sum_i m_i}$, so for the empty universe $\sum_i m_i = 0$ and thus the field equations yield to $0 = 0$, that is a perfectly Machian result.

2. Also for a world with a single particle, although the field equations based on the presented model of inertia predict a solution that is independent of inertial charge and merely depending to the coupling constant μ . But for its geodesic equation the relations (43) and (44) yield to the result $0 = 0$, that means denying any motion for a single particle, an ideal result from a Machian point of view.
3. During the course of the early history of the Universe in the epochs that the phenomena of pair production take place the conditions become prepared to alter the total amount of inertial charge and consequently G . Then keeping the concept of conservation of energy requires that the change of G to be compensated by other source of energy. Here we suppose this can be achieved by requiring the cosmological term to change so that conserves the energy. Indeed this may be considered as dynamical equation that relates the cosmological term to the inertial charges of the Universe i.e.

$$\Lambda_{,\mu} = -\frac{8\pi}{c^4}[GT_{\mu}^{\nu}]_{;\nu} \quad (45)$$

Consequently in the eras of pairs production we have a mechanism to make a large cosmological term which is in agreement with an inflationary scenario.

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References

- [1] Mach, E., *The science of Mechanics*, (The Open Court Publishing Co., 1974).
- [2] Barbour,J., Pfister,H. (Eds.)(1995).*Mach's principle : From Newton's Bucket to Quantum Gravity*, Birkhauser, Boston.
- [3] Abbassi, A. H., Abbassi, A. M., A Modified Theory of Newtonian Mechaincs, J.Sci.I.R.Iran,Vol.7,No.4,277-279,1996. (arXiv:physics/0006021).
- [4] Lynden-Bell, D., A Relative Newtonian Mechanics, ref[3], pp172-178.
- [5] Lynden-Bell,D.,Katz,J., Classical mechanics without absolute space, PRD, Vol.52,No.12,7322-7323,1995.